

Stephen Hawking
and
Quantum Gravity

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Abstract:

Through a combination of his extreme physical limitations, and the equally extreme nature of the subjects of his research, Stephen Hawking has captured a place in the popular imagination.

Quantum gravity in its various incarnations (for example, superstring theory) is now such a widely recognized enigma that many popular books are appearing, including Hawking's own "Brief History of Time".

Many of these books still leave non-experts in the dark.

Just what is involved?

Perceptions:

As is quite common with famous physicists, there is somewhat of a mismatch between the public perception of what he is famous for and the professional opinions of fellow physicists.

(Everyone agrees he's famous.)

Public perception:

- Brief history of time.
- Black holes.
- Baby universes/wormholes.
- Something quantum.

Perceptions:

Professional opinions:

- Singularity theorems (Classical).
- Hawking radiation (Semi-classical).
 - Black hole explosions.
 - Black hole thermodynamics.
 - Black hole geometric entropy.
- Quantum gravity? (Unfinished business).

Brief Biography:

- 1942: Born, Oxford, England.
- 1959: “went up to Oxford” ;
University College (founded 1249).
- 1962: B.Sc. 1st class, U Oxford.
- 1963: Begins Ph.D. with Denis Sciama;
Diagnosis; meets Jane Wilde.
- 1965: Ph.D. U Cambridge;
Marriage (Jane Wilde);
Postdoc: Gonville and Caius [Keys].
- 1967-1970: Singularity theorems
(Classical).

- 1973: Large scale structure (Classical).
- 1974: Black hole explosions (Semi-classical).
- 1974: Inducted Royal Society.
- 1979: Lucasian Professor, Cambridge.
(Inaugural Lecture: End of physics?)
- 1984: (Approx) Quantum gravity.
(Fully quantum; still unfinished business).
- 1985: Trachectomy.
- 1988: Brief History of Time.
- 1990: Divorce (Jane Wilde);
Re-marriage (Elaine Mason).

- 1990s: More quantum gravity.
- 1990s: More books.
- 1990s: String theory.
- 1999: AdS/CFT correspondence (string theory).
- 2000: Braneworld cosmologies.
- 2000: “[Brane new world](#)”.
- 2000: Braneworld inflation.

Health:

Stephen Hawking has “atypical” ALS:

- Amyotrophic Lateral Sclerosis.
- Motor neuron disease.
- Motor neurone disease.
- Lou Gehring’s disease.

Stephen’s comments on ALS:

<http://www.hawking.org.uk>

The classical period:

- The singularity theorems.

Theorem A:

Assume:

1. Classical Einstein gravity.
2. “Energy is always positive” .
3. “The universe is expanding right now” .

Deduce:

1. There is a singularity in our past.
(The Big Bang).
2. “Time had a beginning” .

The classical period:

- The singularity theorems.
1. These are **theorems** of mathematics:
 2. **Assumptions** in \Rightarrow **Conclusions** out.
 3. If you don't like the **Conclusions**, you must reject one (or more) of the **Assumptions**.
 4. But these are pretty basic Assumptions.
 5. Violating any of these Assumptions is almost as interesting as the singularity Theorem itself.

The classical period:

Theorem B:

Assume:

1. Classical Einstein gravity.
2. “Energy is always positive” .
3. “Stars can start to collapse” .

Deduce:

1. “If stars collapse too far, they can’t stop” .
2. Black holes are common, and they contain singularities inside them.

The semi-classical period:

- Black hole explosions?
- Black hole thermodynamics?
- Black hole geometric entropy?

Main points:

- Black holes are not completely black.
- There is a subtle quantum effect that lets energy leak out.
- Temperature proportional to surface gravity.

The semi-classical period:

- Temperature inversely proportional to mass.
- – As it loses mass it gets hotter;
 - it radiates more;
 - loses mass more quickly;
 - finally leading to an explosion?
- “Sorry Stephen, this is all rubbish.”

The quantum period:

- Einstein: “God does not play dice with the universe” .
- Hawking: “God not only plays dice; sometimes He throws them where they cannot be seen” .

What comes out the back end of a black hole explosion?

- Naked singularity?
- Complete evaporation?
- Stable remnant?

The quantum period:

The issue of the final state?

(Of the Hawking evaporation process.)

To answer this question you need to go beyond semi-classical gravity.

You need a full-fledged quantum theory of gravity.

(Because the Hawking temperature has shot up to infinity.)

- Hawking: “Wrong again, Albert.”

The quantum period:

Quantum gravity is an unfinished tapestry:

- Quantum mechanics good.
- General relativity good.
- Put them together: a right proper mess.

Two main candidates:

1. Quantum geometry

[based in the relativity community].

2. M-theory

[*aka* TOE, brane theory, string theory, *nee* dual resonance model].

The Planck scale:

Basic problem: Vacuum fluctuations.

Heisenberg says — (one version of the Uncertainty Principle) —

You can borrow energy from the vacuum provided you pay it back quickly enough:

$$\Delta E \Delta T \leq \hbar.$$

But the energy you borrow will be tightly localized:

$$\Delta L \leq c \Delta T.$$

(Speed of light limitation.)

The Planck scale:

If you borrow enough energy, quickly enough, the vacuum fluctuation will form a (virtual) black hole. This happens when:

$$\frac{G (\Delta E/c^2)}{\Delta L} \geq c^2.$$

Unwrap these equations:

Vacuum fluctuations with

$$\Delta E \geq \sqrt{\frac{G c^5}{\hbar}}$$

should form (virtual) black holes and curdle the vacuum...

This does not seem to happen in real life?

What is going on?

The Cosmological constant:

Problem:

(Just another way of looking at it.)

- The observational astronomers look out into the night sky and measure a (small) non-zero **cosmological constant**.
- The theorists try to calculate it.
- Oops:

$$(Theory) = 10^{123} (Observation).$$

- What is going on?

Conclusion:

- There is an ancient Chinese curse:
- “May you live in interesting times” .
- The times are certainly interesting
- (though I don't think of this as a curse)
- Stephen Hawking is right
in the thick of it.